

# Kerckhoff's Principle in Practice: Addressing Security by Obscurity in Secure Hardware

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+ Thanks to Thomas Roche.



[pyecsca.org](http://pyecsca.org)

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- **Very secretive**
  - NDAs, hard to obtain samples, no docs

# Verifying security

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  - Trust the vendor
  - Security certifications

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**Rarely fails**

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**Vulnerabilities**

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**Here be dragons**

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  - **Common Criteria (+EUCC), FIPS 140, EMVCo**



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- Mandated use of certified products
  - Government, healthcare, eID, ...



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  - Independent lab evaluates

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- Certification that product adheres to some *security target*
  - Independent lab evaluates
- **Certifications reward secrecy**
  - *Attack Potential*
  - Non-public information required -> higher score
  - Samples required -> higher score

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- **EUCLEAK** (2024)
  - Key recovery from EM leakage in ECDSA signing
- All affected certified devices
- All very hard to patch in practice
- Most required recovering non-public information

# Side-channel attacks

- Simple Power Analysis
- Differential Power Analysis
- Correlation Power Analysis
- Mutual Information Analysis
- Refined Power Analysis, Zero-value Point Attack, Exceptional Procedure Attack
- Template attacks
- Leakage assessment
- Doubling attack, Collision attacks
- ...

# Side-channel attacks

is assumed to be known

---

<sup>1</sup> Aurélie Bauer, Eliane Jaulmes, Emmanuel Prouff, Jean-René Reinhard & Justine Wild: Horizontal Collision Correlation Attack on Elliptic Curves

# Side-channel attacks

assumes a white-box evaluator

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<sup>2</sup> Oscar Reparaz, Josep Balasch & Ingrid Verbauwhed: Dude, is my code constant time?

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<sup>3</sup> Johann Heyszl: Impact of Localized Electromagnetic Field Measurements on Implementations of Asymmetric Cryptography

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<sup>4</sup> Pierre-Alain Fouque & Frederic Valette: The Doubling Attack – Why Upwards Is Better than Downwards

# Side-channel attacks

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<sup>5</sup> Bo-Yeon Sim & Dong-Guk Han: Key Bit-Dependent Attack on Protected PKC Using a Single Trace

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<sup>6</sup> Jean-Luc Danger, Sylvain Guilley, Philippe Hoogvorst, Cédric Murdica & David Naccache: A synthesis of side-channel attacks on elliptic curve cryptography in smart-cards

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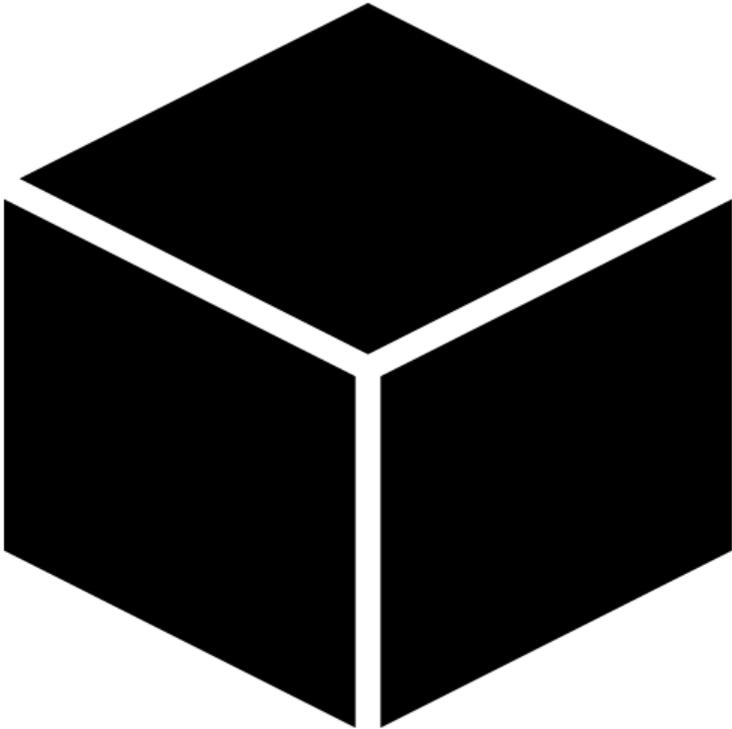
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**Lots of assumptions!**

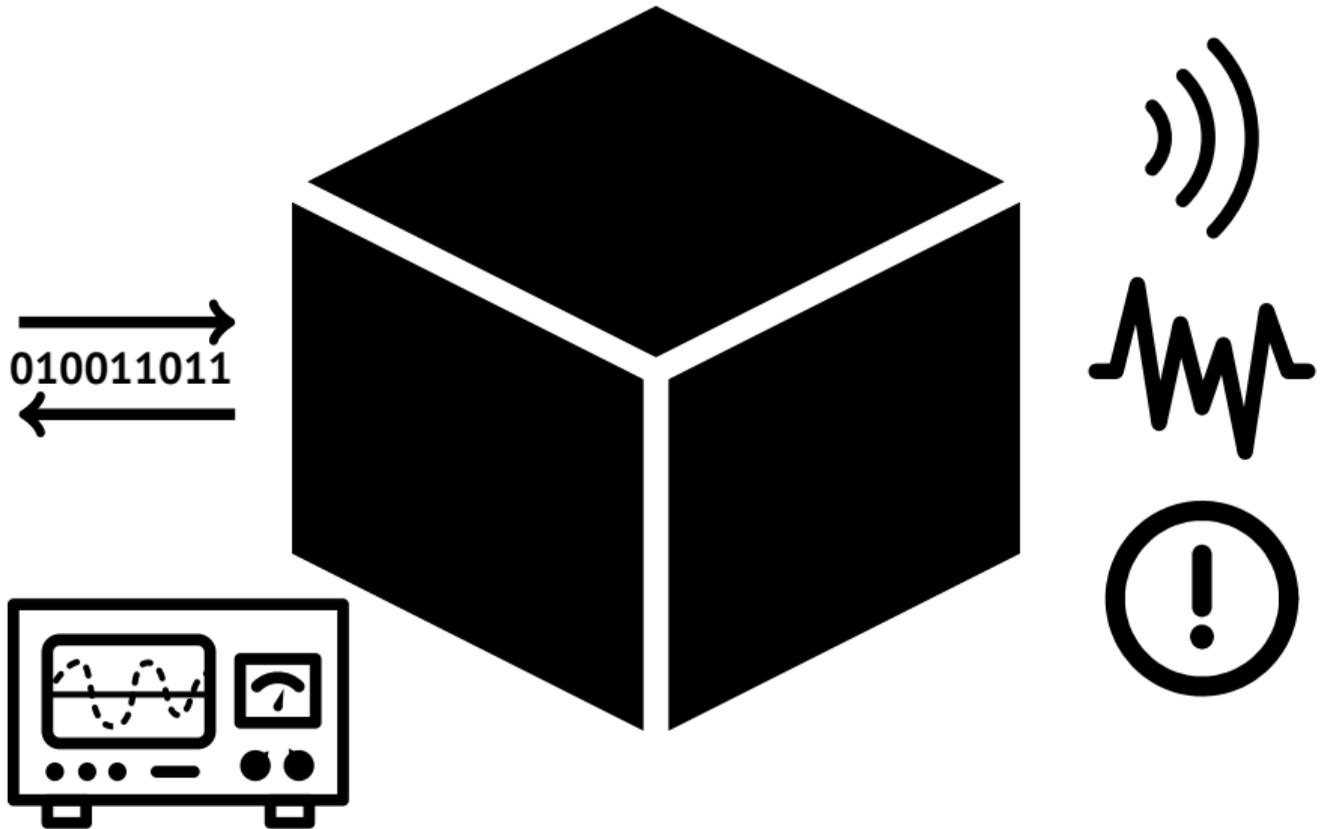
# Reality and the gap

(Kool and the gang)



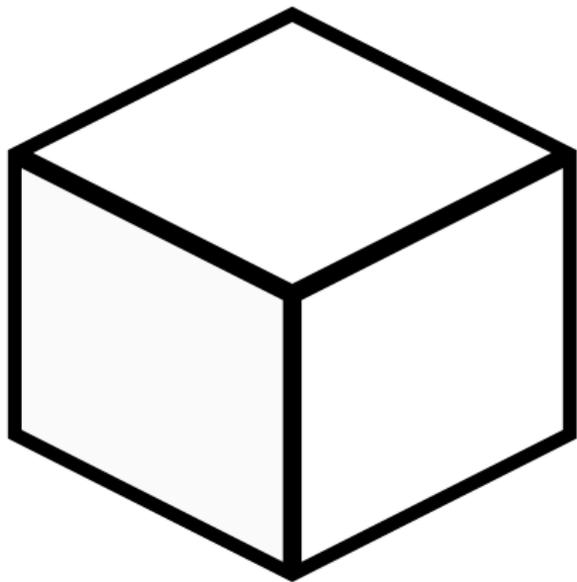
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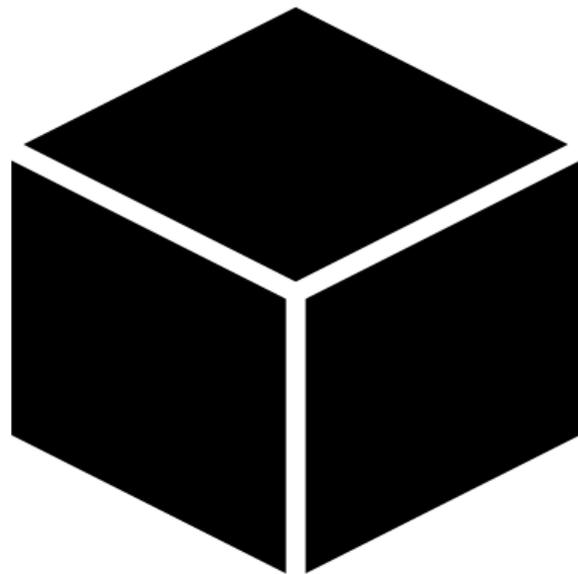
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**Attacks**

**???**

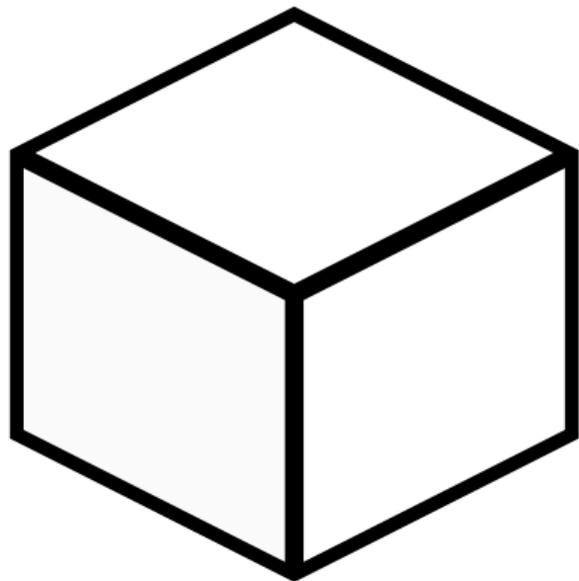
**Security by obscurity**



**Targets**

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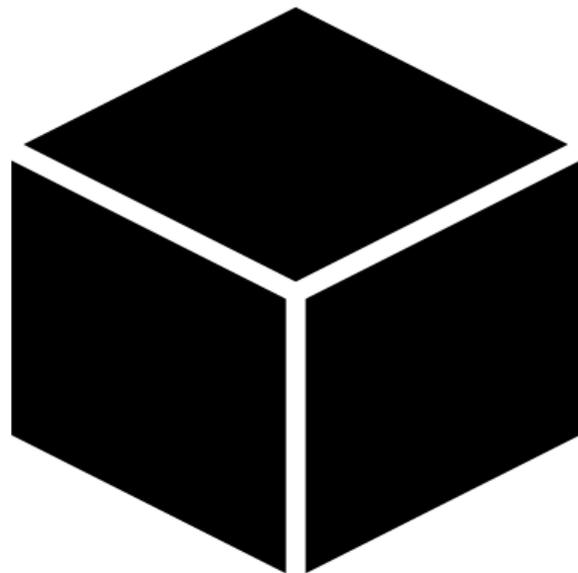


**Attacks**

???

**Security by obscurity**

How large is the gap?  
How hard is it to cross?



**Targets**

# Elliptic curve cryptography

- Many implementation possibilities ...

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  - Curve model
    - ▶  $y^2 \equiv x^3 + ax + b$
    - ▶  $x^2 + y^2 \equiv c^2(1 + dx^2y^2)$
    - ▶  $ax^2 + y^2 \equiv 1 + dx^2y^2$
    - ▶  $by^2 \equiv x^3 + ax^2 + x$

# Elliptic curve cryptography

- Many implementation possibilities ...
  - Curve model
  - Coordinates
    - ▶  $(X, Y)$
    - ▶  $(X, Y, Z)$
    - ▶  $(X, Y, Z, ZZ) \dots$

# Elliptic curve cryptography

- Many implementation possibilities ...
  - Curve model
  - Coordinates
  - Addition formulas

$$Y1Z2 = Y1 * Z2$$

$$U1 = X1 * Z2$$

$$u = Y2 * Z1 - Y1 * Z2$$

$$v = X2 * Z1 - X1 * Z2$$

$$A = u^2 * Z1 * Z2 - v^3 - 2 * v^2 * X1 * Z2$$

$$X3 = v * A$$

$$Y3 = u * (v^2 * X1 * Z2 - A) - v^3 * Y1 * Z2$$

$$Z3 = v^3 * Z1 * Z2$$

$$R = T^2 - U1 * U2 + a * Z^2$$

$$F = Z * M$$

$$L = M * F$$

$$G = T * L$$

$$W = R^2 - G$$

$$X3 = 2 * F * W$$

$$Y3 = R * (G - 2 * W) - L^2$$

$$Z3 = 2 * F * F^2$$

# Elliptic curve cryptography

- Many implementation possibilities ...
  - Curve model
  - Coordinates
  - Addition formulas
  - Scalar multiplier
    - ▶ *LTR, RTL, Window, NAF, Comb ...*

## Fixed-window scalar multiplier

```
function Window( $G, k = (k_l, \dots, k_0)_2$ )  
   $Table = [0G, 1G, \dots, (2^w - 1)G]$   
   $\hat{k} = \text{recode } k \text{ to } w\text{-bit windows}$   
   $T = \mathcal{O}$   
  for  $i = 1$  to  $|\hat{k}|$  do  
     $T = 2^w T$   
     $T = T + Table[\hat{k}_i]$   
  return  $T$ 
```

# Elliptic curve cryptography

- Many implementation possibilities ...
  - Curve model
  - Coordinates
  - Addition formulas
  - Scalar multiplier
  - Finite field operations
    - ▶ Multiplication: *Toom-Cook, Karatsuba, ...*
    - ▶ Squaring: *Toom-Cook, Karatsuba, ...*
    - ▶ Reduction: *Barret, Montgomery, ...*
    - ▶ Inversion: *GCD, Euler*

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- ...that are used in practice
  - Analyzed 18 open-source crypto libraries
  - Mixed curve models
  - Jungle of scalar multipliers (Comb, fixed window, wNAF, GLV, ...)
  - Various coordinate systems
  - Standard and custom addition formulas (more than 100)

# Reverse engineering

- How hard is it to cross the gap?



**pyecsca**

**Side-channels**



**Lying**

# Reverse engineering via side-channel attacks

- 💡 **Idea:** Use side-channel attacks and turn them around
  - ~~Assume knowledge of the impl. and target the key~~
  - Assume knowledge of the key and target the impl.
- ⚡ Behavior of different implementations differs under these attacks

# Reverse engineering via side-channel attacks

- 💡 **Idea:** Use side-channel attacks and turn them around
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  - Assume knowledge of the key and target the impl.
- ≠ Behavior of different implementations differs under these attacks
- Concretely “*special-point-based*” attacks: **RPA, ZVP, EPA**
  - Can recognize when a special point appears in scalar multiplication
  - Introduce zeros adaptively
  - Zeros detectable via side-channel

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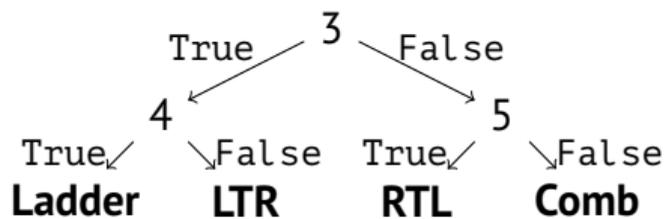
$r =$	2	3	4	5
<b>LTR</b>	True	True	False	False
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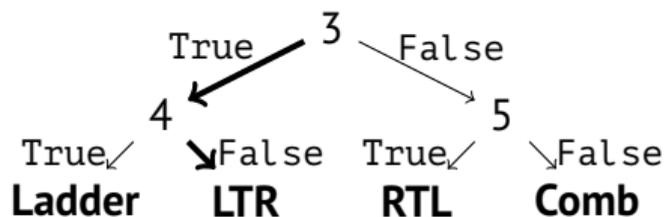


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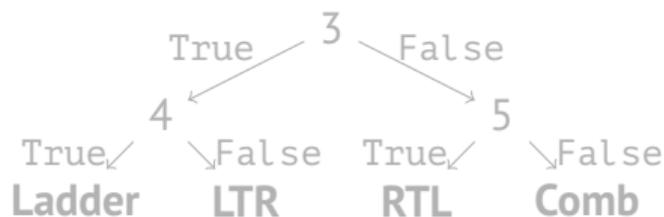
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**Works,**

**but what about countermeasures?**

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# Scalar randomization countermeasures

## Group scalar randomization

```
function Mult( $P, k$ )  
   $r \xleftarrow{\$} \{0, 1, \dots, 2^b\}$   
  return  $[k + rn]P$ 
```

## Additive splitting

```
function Mult( $P, k$ )  
   $r \xleftarrow{\$} \mathbb{Z}_n^*$   
  return  $[k - r]P + [r]G$ 
```

## Euclidean splitting

```
function Mult( $P, k$ )  
   $r \xleftarrow{\$} \{0, 1, \dots, 2^{\lfloor \log_2(n)/2 \rfloor}\}$   
   $S \leftarrow [r]P$   
   $k_1 \leftarrow k \bmod r$   
   $k_2 \leftarrow \lfloor \frac{k}{r} \rfloor$   
  return  $[k_1]P + [k_2]S$ 
```

## Multiplicative splitting

```
function Mult( $P, k$ )  
   $r \xleftarrow{\$} \{0, 1, \dots, 2^b\}$   
   $S \leftarrow [r]P$   
  return  $[kr^{-1} \bmod n]S$ 
```

-> **RPA** will not work

# Reverse engineering by lying

- Countermeasures are correct on well-defined curves, what about bad curves?
- JavaCard platform: Allows any short-Weierstrass curve
- 💡 **Idea:** Recover the countermeasures based on their (erroneous) behavior

## Method 3q

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$$[k]P \quad [k+n]P \quad [k+2n]P$$

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	$[k]P$	$[k+n]P$	$[k+2n]P$
Group scalar	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$
Additive	$\frac{1}{2}$	$\frac{1}{2}$	0
Multiplicative	$\frac{5}{9}$	$\frac{2}{9}$	$\frac{2}{9}$
Euclidean	1	0	0

# Results

Card	Target	Method $3q$			Countermeasure	$r$ bits
NXP 1	Derive	0.34	0.33	0.32	Group scalar	✘
	Sign	0.31	0.31	0.38	Group scalar	160
	Keygen	0.32	0.33	0.35	Group scalar	160
NXP 4	Derive	0.56	0.22	0.22	Multiplicative	64
	Sign	0.54	0.23	0.23	Multiplicative	?
Infineon 2	Derive	0.31	0.36	0.33	Group scalar	✘
	Sign	0.32	0.32	0.36	Group scalar	64
	Keygen	0.32	0.32	0.36	Group scalar	32
...	Many more results in the paper					...

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- Consider transparent alternatives
  -  opentitan
  -  tropic square



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Questions?



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# References

- Jan Jancar, Vojtech Suchanek, Petr Svenda, Vladimir Sedlacek & Łukasz Chmielewski;  
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